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Micro-simulated moving bed (µSMB) systems: A numerical study

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Abstract

Continuous chromatographic separation processes like simulated moving bed (SMB) systems have been employed in petrochemicals, sugar, and more recently, in pharmaceutical industries by virtue of their superior separation efficiency. Miniaturization of chromatography-based analytical techniques (e.g., high performance liquid chromatography, micro-HPLC or μ HPLC) has already been successfully demonstrated in the last few years owing to the rapid development in MEMS technology. With such a rapid progress in technology, it is definitely possible to realize the miniaturization of a powerful continuous chromatographic process such as SMB. Micro-SMB (μ SMB) systems could not only inherit the merits of μ HPLC, but also provide efficient separation of compounds such as isomers and enantiomers that are otherwise very difficult to isolate. In this paper, new simulations of the performance of a μ SMB system for the separation of a mixture of phenol and *o*-cresol, using a robust numerical algorithm developed that mimics the dynamic operation of the μ SMB system, are presented. A systematic parametric sensitivity analysis that addresses the effects of various process parameters on the performance of the μ SMB system is also presented. High purities and yields of both phenol and *o*-cresol is achieved in the μ SMB by judicious choice of process parameters. © 2006 Elsevier B.V. All rights reserved.

Keywords: Chromatography; Micro simulated moving bed; Simulation

1. Introduction

With the revolutionary progress in MEMS technology, miniaturized separation techniques have become very popular in the last few years and they offer numerous advantages over conventional separation processes such as reduced chemical consumption, improved mass sensitivity and separation efficiency [1]. Pregnancy and cholesterol test kits available at home nowadays are essentially micro-labs housing sampling, separation, reaction, and detection units [2]. Many of the separation techniques based on chromatography that are employed in chemical, biomedical and environmental sciences have also been successfully miniaturized. For example, miniaturized versions of high performance liquid chromatography (µHPLC) that are either packed micro-columns [1-4] or surface-functionalized micro monoliths [5,6] have already been demonstrated to isolate species at reduced chemical consumption and with better sensitivity.

Besides being ubiquitously employed as an excellent analytical system, HPLC is widely used in preparative and

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production-scale systems [7,8]. Implementation in productionscale systems necessitates the need for employing continuous chromatographic systems [9]. Simulated moving bed (SMB) [10] and its variant VARICOL[®] [11,12] are two of the conventional yet powerful continuous chromatographic systems that have been successfully implemented in various industrial applications.

A schematic representation of a SMB system is illustrated in Fig. 1 that consists of a number of packed (with adsorbent particles of diameter d_p) columns of uniform cross-section connected in a circular array, each of length L_{col} and diameter d_{col} . The two incoming streams (the feed, F, and the desorbent/eluent, D) and the two outgoing streams (the raffinate, Ra, and the extract, Ex) divide the system into four sections (zones), namely P, O, R and S, each of which is comprised of p, q, r and s columns, respectively. The flow rates in the sections P, Q, R and S are designated as $Q_{\rm P}$, $Q_{\rm O}$, $Q_{\rm R}$ and $Q_{\rm S}$, respectively, while those of the feed, raffinate, eluent/desorbent and extract are designated as $Q_{\rm F}$, $Q_{\rm Ra}$, $Q_{\rm D}$ and $Q_{\rm Ex}$, respectively. However, only four of the above eight flow rates are independent, as the remaining four are determined from the mass balance at points (nodes) A, B, C and D (as shown in Fig. 1). By suitably advancing the inlet and outlet ports, column by column, in the direction of the fluid flow at a pre-set switching time, t_s , the countercurrent movement of the

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Nomenclature

- *a_i* Langmuir isotherm constant of 'i'th component *b_i* Langmuir isotherm constant of 'i'th component (l/mol)
- a_{ii} quadratic isotherm interaction constant (l/mol)
- b_{ij} quadratic isotherm interaction constant (l/mol)²
- \vec{C} liquid phase concentration (mol/l)
- C_0 initial liquid phase concentration (mol/l)
- $D_{\rm ax}$ axial diffusivity (cm²/min)
- $d_{\rm col}$ column diameter (cm)
- $d_{\rm p}$ particle diameter (cm)
- $L_{\rm col}$ column length (cm)
- *m_i* dimensionless solid velocity (based on triangle theory)
- Pe Peclet number
- $P_{\rm P}$ purity of phenol (%)
- $P_{\rm C}$ purity of *o*-cresol (%)
- q_{\perp} concentration in the solid phase (mol/l)
- q^* concentration at solid phase in equilibrium with mobile phase (mol/l)
- $Q_{\rm F}$ feed flow rate (ml/min)
- Q_i flow rate in section '*i* = P, Q, R, S' (ml/min)
- $t_{\rm s}$ switching period (min)
- $U_{\rm F}$ fluid interstitial velocity (cm/min)
- $V_{\rm col}$ column volume (cm³)
- $Y_{\rm P}$ yield of phenol (%)
- $Y_{\rm C}$ yield of *o*-cresol (%)

Greek letters

- $\begin{array}{ll} \alpha & \mbox{lumped mass transfer coefficient (min^{-1})} \\ \alpha_{\rm m} & \mbox{lumped dimensionless mass transfer coefficient} \\ \varepsilon & \mbox{bed porosity} \\ \nu & \mbox{solid to fluid volume ratio} \\ \zeta & \mbox{solid velocity} \\ \chi & \mbox{dimensionless length} \\ \theta & \mbox{dimensionless time} \\ \hline Superscripts and subscripts \\ \end{array}$
- D desorbent or eluent Ex extract F feed P, Q, R, S sections of the SMB Ra raffinate

solids is simulated. This switching time is the key parameter, which defines the hypothetical solid velocity ($\zeta \sim L_{col}/t_s$). However, the countercurrent separation of the components could be achieved only by judiciously specifying the internal flow rates in the columns besides the switching time.

An exhaustive literature is available on conventional SMB systems. Theories like McCabe-Thiele method [9], triangle theory [13,14], and standing wave design [15] have also been developed over the years that have become quite popular in the operability design of SMB systems. Researchers have successfully demonstrated using SMB to obtain high purity and yield of



Fig. 1. A schematic representation of a four zone (two columns per zone) SMB system.

species from a variety of mixtures that include aromatics [16], sugars [17–19], and more recently enantiomers [11,12,20–23]. Several researchers have also reported design and optimization methodologies [13–16,18,19,21,24,25] to achieve optimal separation using SMB. Attempts have also been successful in employing SMB as an in situ reactor-separator [26–28].

2. Micro-simulated moving bed (µSMB) system

Enantiomers, which are routinely used in pharmaceuticals, have near unity partition coefficients and are very difficult to isolate. As mentioned earlier, SMB systems have been proven to be highly effective in isolating components like isomers and enantiomers (with partition coefficient \rightarrow 1) that are difficult to separate via other chromatographic techniques. Not only that these compounds are very expensive but also the adsorbents and eluents/desorbents used in SMB are very costly. Hence, there is always a need for reduction in the volume of columns, con-

Table 1

Operating and adsorption parameters for single column elution in conventional HPLC [30]

L _{col} (mm)	150.0	
$d_{\rm col} (\rm mm)$	3.3	
$d_{\rm p}$ (µm)	7.0	
$\hat{V_i}$ (µl)	550.0	
Q_i (ml/min)	1.0	
$C_{0,\mathrm{P}} \pmod{l}$	0.1	
$C_{0,C}$ (mol/l)	0.1	
v (-)	0.49	
<i>a</i> ₁ (–)	5.4	
<i>a</i> ₂ (–)	12.48	
$b_1 (\text{mol/l})^{-1}$	2.85	
$b_2 (\text{mol/l})^{-1}$	7.5	
$a_{12} (\text{mol/l})^{-1}$	11.7	
$a_{21} (\text{mol/l})^{-1}$	-12.8	
$b_{12} (\text{mol/l})^{-2}$	-10.69	
$b_{21} (\text{mol/l})^{-2}$	-24.7	



Fig. 2. Simulated concentration elution profile in a conventional HPLC for phenol and *o*-cresol obtained at experimental conditions (cf. Table 1) reported by Jandera et al. [30]. Separon SGX C_{18} microparticles (7 µm) is the packing material and 30% (by volume) of methanol in water is the desorbent.

Table 2 Operating and adsorption parameters for single column elution in μ HPLC [4]

$\overline{L_{\rm col} \ (\rm mm)}$	143.0
$d_{\rm col}~(\mu {\rm m})$	320.0
<i>d</i> _p (μm)	5.0
V_i (µl)	5.5
Q_i (µl/min)	5.0
$C_{0,\mathrm{P}} \pmod{l}$	0.1
$C_{0,C}$ (mol/l)	0.1
υ (-)	0.44
<i>a</i> ₁ (–)	3.87
<i>a</i> ₂ (–)	5.52
$b_1 (\text{mol/l})^{-1}$	0.49
$b_2 (\text{mol/l})^{-1}$	2.05

sumption of eluent and yet maintain high purity and yield of product species. Inspired by the recent works on miniaturization of HPLC columns [1–6], an attempt has been made in this paper, to investigate the performance of a micro-SMB (μ SMB) system by numerical simulations. Micro-SMB systems, apart from inheriting the various afore-mentioned advantages of the μ HPLC columns, can also be very effective in separating compounds that are very difficult to isolate via other separation techniques. Also with a better understanding of the performance of μ SMB systems, one can envision the possibility of integrating the μ SMB system as a reactor-separator given that conventional SMB has already been demonstrated to efficiently serve as an in situ reactor-separator [26–28].



Fig. 3. Simulated concentration elution profile in a μ HPLC for phenol and *o*cresol obtained at experimental conditions (cf. Table 2) reported by Jandera et al. [4]. Separon SGX C₁₈ microparticles (5 μ m) is the packing material and 50% (by volume) of methanol in water is the desorbent.

Table 3			
Reference process	parameters	for	μSMB

$\overline{L_{\rm col}~(\rm mm)}$	50.0
$d_{\rm col}~(\mu {\rm m})$	320.0
$d_{\rm p}$ (µm)	5.0
p, q, r, s (column configuration)	1, 2, 2, 1
$Q_{\rm P}$ (µl/min)	20.0
$Q_{\rm Q}$ (µl/min)	15.34
$Q_{\rm R}$ (µl/min)	15.4
$Q_{\rm S}$ (µl/min)	12.0
$C_{0,\mathrm{P}} \; (\mathrm{mol/l})$	0.1
$C_{0,\mathrm{C}} \pmod{1}$	0.1
v (-)	0.44
α (min ⁻¹)	150.0
<i>a</i> ₁ (–)	3.87
<i>a</i> ₂ (–)	5.52
$b_1 (\text{mol/l})^{-1}$	0.49
$b_2 ({\rm mol/l})^{-1}$	2.05

The primary goal of the present study is to systematically study the influence of different process parameters on the performance of the μ SMB system. The separation of a binary mixture of phenol and *o*-cresol using 50% (by volume) methanol in water as the eluent over Separon SGX C₁₈ microparticles (5 μ m) as adsorbent [4] is chosen as the model system in the present study. Phenol is the weakly adsorbed species and hence collected from the raffinate stream, while *o*-cresol is the strongly adsorbed one which is collected from the extract stream. In what follows, the



Fig. 4. Simulated concentration profiles in a μ SMB system for phenol and *o*cresol at cyclic steady state: (a) start; (b) middle; and (c) end of the switching period ($t_s = 0.52$ min). The process parameters are listed in Table 3.

development and validation of the numerical algorithm for the μ SMB system is discussed. The parametric sensitivity of various process parameters such as the switching time (t_s), number of columns (p, q, r, s) in each section (P, Q, R, S) of the μ SMB, the different section flow rates (Q_P, Q_Q, Q_R, Q_S) on the performance of the μ SMB system is then discussed. Finally, the concluding remarks and the outlook of future research are presented.

3. Numerical model

A mathematical model that has been proven to mimic conventional SMB systems [16,18,19] very well is employed in the present study to capture the dynamic behavior of the μ SMB system. The differential transient mass balance equations along with the boundary conditions are as follows:

$$\frac{\partial C_{i,k}}{\partial \theta} + \upsilon \frac{\partial q_{i,k}}{\partial \theta} = \frac{\psi_k}{Pe_k} \frac{\partial^2 C_{i,k}}{\partial \chi^2} - \psi_k \frac{\partial C_{i,k}}{\partial \chi}$$
(1)

$$\frac{\partial q_{i,k}}{\partial \theta} = \alpha_{\rm m} (q_{i,k}^* - q_{i,k}) \tag{2}$$

where $C_{i,k}$ is the concentration of the '*i*'th species in the liquid in the '*k*'th column, $q_{i,k}^*$ the concentration in the solid phase in equilibrium with that in the liquid, $q_{i,k}$ the concentration in the solid, $\chi = z/L_{col}$ the dimensionless length, $\upsilon = (1 - \varepsilon)/\varepsilon$ the ratio of volumes of solid to liquid phases, ε the bed porosity, $\alpha_{\rm m} = t_{\rm s} \alpha$ the dimensionless mass transfer coefficient and $\theta = t/t_{\rm s}$



Fig. 5. Effects of switching time (t_s) and mass transfer coefficient (α) on the performance of μ SMB system. Reference parameters are listed in Table 3.

is the dimensionless time. The other dimensionless parameters in the above equations are the ratio of liquid to solid velocities $(\psi_k = U_{F_z} t_s / L_{col})$ and Peclet number $(Pe_k = U_{F_k} L_{col} / D_{ax_k})$.

As the column diameter is decreased, the adsorption isotherm parameters of the different species, though being thermodynamic properties, change due to differences in packing density and inaccurate measurements of extra-column volumes [4]. Hence, adsorption isotherms measured using conventional HPLC columns may not hold good for μ SMB system. Jandera et al. [3,4,29] and Jandera and Komers [30] reported a series of systematic measurements of isotherms using various conventional and packed μ HPLC columns. In the present study, either a competitive Langmuir isotherm (Eq. (3)) obtained from a μ HPLC column [4] or a competitive quadratic isotherm (Eq. (4)) [30] (for the validation of the algorithm) reported by Jandera et al. is used to describe the multi-component adsorption equilibria.

$$q_{i,k}^* = \frac{a_i C_{ik}}{1 + \sum_{j=1}^2 b_j C_{jk}}$$
(3)

$$q_{i,k}^{*} = \frac{a_i C_{ik} + a_{ip} C_{ik} C_{pk}}{1 + \sum_{j=1}^{2} b_j C_{jk} + b_{ip} C_{ik} C_{pk}}; \quad (p \neq i)$$
(4)

The boundary conditions are:

$$C_{i,\chi}^{\rm in} = C_{i,k}(0,\,\theta) - \frac{1}{Pe_k} \frac{\partial C_{i,k}}{\partial \chi}$$
(5)

$$\frac{\partial C_{i,k}}{\partial \chi}(1,\,\theta) = 0\tag{6}$$

The initial conditions are:

$$C_{i,k}(\chi, 0) = C_{i,k}^0(\chi)$$
 and $q_{i,k}(\chi, 0) = q_{i,k}^0(\chi)$ (7)

The mass balance at the node is then,

$$C_{i,k}^{\text{in}} = C_{i,k-1}(1,\,\theta)$$
 (8)



Fig. 6. Effects of number of columns (p and q) in sections P and Q, respectively, on the performance of µSMB system. Reference parameters are listed in Table 3.

except if the column follows feed or desorbent port in which case,

$$C_{i,k}^{\text{in}} = \frac{[Q_{\text{F}}C_{i,\text{F}} + Q_{\text{Q}}C_{i,k-1}(1, \theta)]}{Q_{\text{R}}} \quad \text{and} \\ C_{i,k}^{\text{in}} = \frac{Q_{\text{S}}C_{i,k-1}(1, \theta)}{Q_{\text{P}}}, \tag{9}$$

respectively.

The resulting system of PDEs are discretized in space using the finite difference approximations to convert them into a system of coupled ODE-IVPs (Method of Lines) [22,27,28]. Each column length is spatially discretized using 100 grid points. These stiff initial value ODEs were solved using a robust algorithm developed in FORTRAN90 along with the subroutine, DIVPAG (based on Gear's method), in the IMSL library. Since a periodic switching is imposed on the system, the µSMB system operates under transient conditions. However, a cyclic (periodic) steady state with a period equal to the global switching time is eventually reached after several switchings. For the system studied in this paper, a periodic steady state is attained after about 150 switching cycles. High mass transfer rates are assumed and the Peclet number is calculated using the commonly used correlation [31]. The purities (%) of phenol and *o*-cresol are designated as P_P and P_C , respectively, while their yields (%) are denoted by Y_P and Y_C , respectively. The definitions of the purity and yield of the two species, respectively, are as follows:

$$P_{\rm P} = \frac{C_{\rm P}^{\rm Ra}}{C_{\rm P}^{\rm Ra} + C_{\rm C}^{\rm Ra}} \times 100 \tag{10}$$

$$P_{\rm C} = \frac{C_{\rm C}^{\rm Ex}}{C_{\rm P}^{\rm Ex} + C_{\rm C}^{\rm Ex}} \times 100 \tag{11}$$

$$Y_{\rm P} = \frac{Q_{\rm Ra} C_{\rm P}^{\rm Ra}}{Q_{\rm F} C_{0,\rm P}} \times 100$$
(12)

$$Y_{\rm C} = \frac{Q_{\rm Ex} C_{\rm C}^{\rm Ex}}{Q_{\rm F} C_{0,\rm C}} \times 100 \tag{13}$$

The algorithm developed is benchmarked by first simulating the single-column elution curves of phenol and *o*-cresol in a HPLC column (3.3 mm) at the experimental process parameters (cf. Table 1) reported by Jandera and Komers [30]. Fig. 2 clearly elucidates that the simulated elution curves are in excel-



Fig. 7. Effects of number of columns (r and s) in sections R and S, respectively, on the performance of µSMB system. Reference parameters are listed in Table 3.

lent agreement with the experimental curves [30]. Jandera et al. [4] also reported adsorption isotherms of phenol and *o*-cresol obtained from a micro-HPLC column (320 μ m). Though the authors reported the experimental process parameters for the single column elution measurements (cf. Table 2), they did not report the elution curve which could have been beneficial to benchmark the present algorithm. For completeness, the simulated elution curves in a μ HPLC column at the experimental conditions listed in Table 2 [4] are illustrated in Fig. 3. Clearly, the separation (Fig. 3) under the experimental conditions is not as efficient as that from the conventional HPLC column (Fig. 2).

4. Results and discussion

Mazzotti et al. [13,14] have shown through the now-sopopular triangle theory that complete separation is possible if the dimensionless solid velocity m_i (*i* = P, Q, R, S) in the different sections of SMB satisfies a set of inequalities.

$$m_i = \frac{Q_i t_{\rm s} - V_{\rm col}\varepsilon}{V_{\rm col}(1 - \varepsilon)} \tag{14}$$

Following the triangle theory [13,14], a series of simulations are performed to find out a set of process parameters for the µSMB system where complete separation of phenol and ocresol is achieved. A switching period (t_s) of 0.52 min for the μ SMB system ($L_{col} = 5 \text{ cm}, d_{col} = 320 \text{ }\mu\text{m}, d_{p} = 5 \text{ }\mu\text{m}, \upsilon = 0.44$) that consisted of a column configuration of 1-2-2-1 in the P, Q, R, and S sections, respectively, and other judicious choice of process parameters (cf. Table 3) satisfies the constraints of the triangle theory for the competitive Langmuir isotherm [4] which aptly describes the distribution of phenol and o-cresol in the solid and liquid phases. Fig. 4 elucidates the simulated concentration profiles of phenol and o-cresol (under the afore-mentioned conditions; also as listed in Table 3) in the four different sections of the μ SMB system at the beginning (see Fig. 4(a)), middle (Fig. 4(b)) and end of the switching period (Fig. 4(c)) after cyclic steady state is attained. Fig. 4 clearly shows that complete sep-



Fig. 8. Effects of flow rates in sections P and Q, respectively, on the performance of µSMB system. Reference parameters are listed in Table 3.

aration of the two species (100% purity and yield of phenol and o-cresol, respectively), is achieved. Under the flow conditions as given in Fig. 4, achieving the desired pressure drop for flow through micro-columns is of prime importance. However, using the classical Ergun's equation [32], the pressure drop between the ends of the columns of the μ SMB system is determined to be of the order of 1 atm, which can be readily achieved by the instrumentation described by Jandera et al. [3,4,29] and Jandera and Komers [30].

The variations in performance of the μ SMB with changes in switching period (t_s) and mass transfer coefficient (α) at fixed values of all other process parameters (cf. Table 3) are elucidated in Fig. 5. Clearly, there is an optimal value of t_s at which both phenol and *o*-cresol are separated with 100% purity and yield, respectively. Under the reference conditions, complete separation is achieved with a switching period of 0.52 min. However, when t_s is slightly changed to 0.47 min, both the species are not obtained at 100% purity. As expected, as the mass transfer coefficient (α) is increased, complete separation is achieved when $t_s = 0.52$ min. Also, it is evident from Fig. 5 that even at high α , when $t_s = 0.47$ min, complete separation is not achieved.

Figs. 6 and 7 illustrate the effect of the number of columns in the different sections on the performance of µSMB system at two different t_s while holding the other process parameters constant (cf. Table 3). When $t_s = 0.52 \text{ min}$, the number of columns in all the sections (P, Q, R and S) hardly affects the system performance and always complete separation is achieved. However, when section R (feed section) consists of only one column (with other parameters fixed) at $t_s = 0.52$ min, the solid volume in the feed section is not enough to completely adsorb o-cresol and hence the purity of phenol is affected (cf. Fig. 7). Also it is evident from Figs. 6 and 7 that the system performance is severely affected by the change in the number of columns when $t_s = 0.47$ min. Both components are not obtained at 100% purity and yield in this case. While the purity and yield of one of the components is improved, those of the other component are diminished, which implies that there is a complex interplay of the various process parameters on the performance of the µSMB system.



Fig. 9. Effects of flow rates in sections R and S, respectively, on the performance of µSMB system. Reference parameters are listed in Table 3.

The change in the system performance with variations in the different section flow rates (at constant values of other parameters listed in Table 3) at two different t_s is explicated in Figs. 8 and 9. Again, the system performance is mostly superior when $t_s = 0.52$ min compared to that when $t_s = 0.47$ min. The variations in the internal flow rates in sections P and S do not affect the purity and yield of both species significantly when $t_{\rm s} = 0.52$ min. Complete separation is achieved for a wide range of $Q_{\rm P}$ and $Q_{\rm S}$ at $t_{\rm s} = 0.52$ min. However, the variations in the flow rates Q_Q and Q_R significantly affect the purity and yield of the two components even when $t_s = 0.52 \text{ min.}$ Low (high) values of Q_Q (Q_R), holding other parameters constant, causes (implies) an increase in the feed flow rate (Q_F) that can be too high to be handled by the volume of adsorbent in section R thereby hampering the purity (as low as 50%) and yield (as low as 20%) of both components (cf. Figs. 8 and 9). However, it is evident from Fig. 9 that when $t_s = 0.47$ min, as Q_R is increased, the system performance is superior compared to that when $t_s = 0.52$ min. This could be attributed to the increase in solid phase velocity ($\zeta \sim L_{col}/t_s = 10.64$ cm/min) due to the small t_s (at high $t_s = 0.52$ min, $\zeta \sim 9.62$ cm/min) which compensates for the increase in feed flow rate (Q_F).

It is also imperative to find out if there is any room for reduction in the volume of the columns (by decreasing L_{col}) and still achieve complete separation of the product species. Also it is essential to see if complete separation can be achieved with changes in the feed concentration. Fig. 10 elucidates the effect of the variations in α at two different L_{col} (at other constant parameters listed in Table 3) on the purity and yield of phenol and *o*-cresol. When L_{col} is 3 cm, t_s is set to be 0.31 min so that the solid phase velocity (ζ) is still maintained at 9.62 cm/min (which is the case when $L_{col} = 5$ cm and $t_s = 0.52$ min). This ensures that



Fig. 10. Effects of α (for different L_{col}) and feed concentration (C_0) on the performance of μ SMB system. For each L_{col} , t_s is chosen such that $\zeta = 9.62$ cm/min. Other reference parameters are listed in Table 3.

at the reference values of all other parameters, the μ SMB system provides complete separation of the components (cf. Fig. 10). However, it is worth noting that the decrease in length of the column is also subjected to the experimental constraints as the operation of μ SMB involves complicated instrumentation. Also shown in Fig. 10 is the effect of changes in feed concentration (C_0) on the system performance. It is evident from Fig. 10 that as the feed concentration of both the components is increased (by equal amounts), the purity and yield of one of the species always gets diminished. This reiterates the fact that the performance of the μ SMB system is strongly influenced by the complex interplay of the various process parameters.

5. Conclusions

Numerical simulations presented in this paper capture the dynamic behavior of a novel μ SMB system for the separation of a model system (viz., a mixture of phenol and *o*-cresol). Judicious choice of process parameters based on triangle theory [13,14] provides complete separation of phenol and *o*-cresol. However, the performance of the μ SMB system is affected in a complex manner by various process parameters. Slight changes in the process parameters result in the decrease in purity and yield of at least one of the species in some cases and in the worst scenario, affects both the species. A systematic and comprehensive optimization study needs to be performed to achieve optimal operation of the μ SMB system. Experimental validation is yet another and important logical step.

Drawing inspiration from the MEMS community, where researchers aim at developing integrated micro-devices to enhance the throughput, the integration of the μ SMB systems could be envisaged as an option. Also, the μ SMB system has the potential to serve as an in situ reactor-separator (like conventional reactive SMB systems [26–28]), which could open new avenues for the micro-reactor research community.

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